Symbolic Verification of Regular Properties

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ABSTRACT
Verifying the regular properties of programs has been a significant challenge. This paper tackles this challenge by presenting symbolic regular verification (SRV) that offers significant speedups over the state-of-the-art. SRV is based on dynamic symbolic execution (DSE) and enabled by novel techniques for mitigating path explosion: (1) a regular property-oriented path slicing algorithm, and (2) a synergetic combination of property-oriented path slicing and guiding. Slicing prunes redundant paths, while guiding boosts the search for counterexamples. We have implemented SRV for Java and evaluated it on 15 real-world open-source Java programs (totaling 259K lines of code). Our evaluation results demonstrate the effectiveness and efficiency of SRV. Compared with the state-of-the-art — pure DSE, pure guiding, and pure path slicing — SRV achieves average speedups of more than 8.4X, 8.6X, and 7X, respectively, making symbolic regular property verification significantly more practical.

1 INTRODUCTION
Regular properties are ones that can be specified by finite state machines (FSMs) [22]. They are widely used for property specification in software analysis and verification (e.g., model-based testing [36], typestate analysis [21], model checking [14], and performance analysis [33]). However, scalable regular property verification is difficult, and practical verification of regular properties of real-world programs is a significant software engineering research challenge.

Two main lines of research exist on regular property verification: static and dynamic verification. Static verification (such as [17, 20, 21]) soundly abstracts programs for verification, which usually has high code coverage, but suffers from false alarms. Dynamic verification (such as [2, 12]), in contrast, executes the program and monitors program executions online. Hence, dynamic verification ensures completeness, i.e., every discovered violation is real. However, dynamic approaches only verify a program’s behavior under specific inputs, thus may miss bugs.

Symbolic execution [10, 23, 30] achieves trade-offs between static and dynamic verification by using symbolic values for program execution. A key step in symbolic execution is to explore all possible cases when encountering a branch via forking states or re-executing the program. Compared with static and dynamic approaches, symbolic execution achieves better precision or coverage, respectively.

Our goal is to develop a practical technique for symbolic regular property verification. At the high-level, it works as follows. For a regular property $\varphi$ and program $P$, an event in $\varphi$’s FSM represents the execution of one or more statements of $P$. For example, a method invocation may produce an event. Hence, w.r.t. $\varphi$, an execution path $p$ of $P$ generates an event sequence, denoted as $\text{Seq}(p)$. If $\text{Seq}(p)$ is empty, $p$ is an irrelevant path; otherwise, $p$ is relevant. To verify that $P$ satisfies $\varphi$, we adopt symbolic execution to explore $P$’s path space. If there exists a path $p$ that violates $\varphi$, i.e., $\text{Seq}(p)$ is accepted by the FSM of $\neg \varphi$ (denoted by FSM$_{\neg \varphi}$), a violation is found, and $p$ is a counterexample path. Otherwise, $P$ satisfies $\varphi$.

However, symbolic execution is hindered by the problem of path explosion — exponential path space w.r.t. the number of branches in the program. Thus, how to steer symbolic execution to (1) completely explore the path space and (2) find counterexamples as soon as possible is critical. This paper tackles these challenges and introduces a scalable verification technique, called symbolic regular verification (SRV), for regular properties via dynamic symbolic execution (DSE) [23, 41]. SRV is inspired by two key observations. First, there usually exist a large number of irrelevant paths in $P$ w.r.t. the regular property $\varphi$. Second, many of the relevant paths in $P$ are equivalent, i.e., the paths having identical event sequence w.r.t. $\varphi$. Therefore, during DSE, it is desirable to (1) prune both irrelevant and equivalent relevant paths, and (2) explore counterexample paths as early as possible. Doing these can boost symbolic verification to find counterexamples and finish path exploration more promptly.

To verify a regular property $\varphi$ for a program, the key idea of SRV is to (1) slice a path w.r.t. related statements of $\varphi$, which results in
The verification framework combines regular property-oriented path slicing and the property-oriented guiding technique [49] in a synergistic manner, in which the combined techniques complement and also boost each other.

We have implemented SRV for Java utilizing a regular property guided symbolic execution engine [47] and a dynamic slicing tool Javaslicer [15]. SRV has been extensively evaluated on 15 real-world open-source Java programs using regular properties involving both single or multiple objects. The evaluation results demonstrate SRV’s effectiveness and efficiency for regular property verification.

This paper makes the following main contributions:

- A property-oriented path slicing algorithm that can prune paths for verification w.r.t. regular properties. The explored paths using our slicing algorithm is two orders of magnitude less than that using path slicing [27][16].
- A DSE-based framework that integrates slicing and guiding for practical regular property verification.
- A prototype implementation for Java that significantly outperforms the state-of-the-art: (1) successfully verified 30 out of 39 verification tasks on a total of 259K lines of code within 1 hour, while pure DSE, guiding, and path slicing verified 22/22/23 tasks, respectively; and (2) on the 30 successfully verified tasks, offered more than 8.4X/8.6X/7X average speedups over pure DSE, guiding, and path slicing, respectively.

The rest of this paper is organized as follows. Section 2 motivates and illustrates symbolic regular verification (SRV) via a concrete example, and Section 3 presents the details of SRV. Section 4 explains our implementation and experimental evaluation of SRV. Finally, we survey related work (Section 5) and conclude (Section 6).

2 ILLUSTRATING EXAMPLE

This section uses an example to motivate and illustrate our symbolic regular property verification technique. Figure 1 shows a Java program snippet that uses an Iterator to access an ArrayList. The input parameters are an ArrayList arr and an integer variable m. First, we increase m by 1 if m is greater than 10. Then, we obtain arr’s iterator, and assign it to iter. The following for loop (Lines 6-9) finds the maximum value of the first half of arr, and stores it in max. Next, max will be removed from arr if its value equals 100. The following while loop (Lines 12-16) iterates arr by using the iterator iter. During the iteration, we update the value of max to the value of an element if the element is bigger than max. Finally, the addition of m and max is returned.

```java
public int test(ArrayList<Integer> arr, int m){
    if(m > 10) //qs
        m++;//q0
    int max=0; //q0
    Iterator iter=arr.iterator(); //q1 - q4
    for(int i = 0; i < arr.size()/2; i++){ //i.hasNext
        q4
        max = arr.get(i).intValue(); //q4 - q5
    }
    //q5 - q6
    if(max == 100) //q6
        arr.remove(max); //q6 - q7
    while(iter.hasNext()) //i.hasNext
    int temp = iter.next(); //i.hasNext
    max = temp; //q7 - q8
    return m+max; //q8
}
```

For the motivation program, we are interested in the correct usage of a collection’s Iterator, i.e., the collection cannot be modified while being iterated and the iterator should invoke method hasNext before next. Note that such a safety property involves two objects. The property can be specified as a regular property \( \varphi \), and FSM\(_{\varphi}\) is shown in Figure 2, where \( a \) and \( i \) represent an ArrayList object and the corresponding iterator object, respectively. For brevity, we use \( a.update \) to represent adding an element to \( a \) or removing an element from \( a \). Event \( a.iterator \) denotes the accessing of \( a \)’s iterator. We use \( i.hasNext \) and \( i.next \) to represent invoking the method hasNext and next, respectively. Obviously, when the first half of ArrayList has an element that equals 100, a violation of \( \varphi \) occurs, i.e., the ArrayList removes an element while being iterated. In this paper, we assume that every event is atomic, i.e., no other events may be generated during its execution.

![Figure 1: An example program.](image1)

![Figure 2: The FSM of iterator bug involving multi-objects.](image2)
data flow analysis to calculate the future behavior information, called \textit{Postset}, of every program location. A \textit{Postset} of a location \textit{loc} contains some states of FSM_{\textit{loc}}, and each state \textit{q} indicates that there may exist a subsequent path \textit{p} after \textit{loc} and Seq(p) can drive FSM_{\textit{loc}} from \textit{q} to an accepted state. The comment of each line in Figure 1 shows the \textit{Postset} of the location after the line. For brevity, we use \{q_1 \sim q_k\} to represent \{q_j \mid j \leq l \leq k\}. For example, after Line 10, there exists a subsequent path \textit{p} that Seq(p) = ⟨\textit{update}, hasNext, next⟩, which can drive \textit{q_1} to the accepted state. Hence, the \textit{Postset} of the location after Line 10 contains \textit{q_1}.

At the second stage, the program will be analyzed via DSE. During DSE, the \textit{Postset} information calculated earlier will be used to select the paths to explore. Because DSE also runs the program concretely, we can use the available runtime information to calculate certain history information, called \textit{Preset}, of a branch to be explored. Same as \textit{Postset}, the \textit{Preset} of a branch \textit{b} also contains some states of FSM_{\textit{b}}. A state \textit{q} in \textit{Preset} indicates that \textit{q} can be reached from the initial state via the path from the beginning of the program to \textit{b}. Based on the \textit{history} and \textit{future} information, we can (1) prune the redundant program paths, which include irrelevant paths, non-counterexample paths and the equivalent paths of previously explored paths; and (2) evaluate the possibility of a branch for generating a counterexample path.

When a path \textit{p} is explored by DSE, property-oriented path slicing is employed on \textit{p} to slice the branches w.r.t. \textit{ϕ}. Slicing uses static dependence analysis [27] and the \textit{history} and \textit{future} information to reason about possibly accepted event sequences along a branch. If a branch \textit{b}'s intersection of the \textit{Preset} and \textit{Postset} is empty, it means no counterexample path along \textit{b} exists. Besides, if all the counterexample paths along \textit{b} have equivalent paths explored previously, it is also no need to explore \textit{b}. Under both of these conditions, \textit{b} will be pruned, which results in pruning all the paths along \textit{b}. On the other hand, we also use the intersection of the \textit{Preset} and \textit{Postset} to calculate the heuristic value of \textit{b}. If the size of the intersection is larger, the possibility of having a counterexample path along \textit{b} is considered higher. Hence, \textit{b} will be selected with a higher priority.

Consider the program in Figure 1 and the FSM_{\textit{b}} in Figure 2. To analyze the program via DSE, the two input parameters are made symbolic variables. We assume that the \textit{arraylist} \textit{arr} has a fixed length and contains two elements \textit{arr}[0] and \textit{arr}[1]. Suppose the initial input to test is \langle arr = [1, 2], \textit{m}=3 \rangle. The first iteration generates the event sequence ⟨\textit{iterator}, hasNext, next, hasNext, next, hasNext⟩, and is not a counterexample path. Figure 3 shows the execution tree after the first iteration, where \textit{dashed} states are candidate states to explore. The \textit{Preset} and \textit{Postset} of a candidate branch are above and below the branch, respectively. For example, \textit{b_3} corresponds to the true branch of Line 10, and \textit{b_3}'s \textit{Preset} and \textit{Postset} are \{q_1\} and \{q_1, q_2, q_3, q_4\}, respectively. The \textit{pruned} candidate branches are \textit{dashed} and \textit{grey}, while the remaining are \textit{dotted} and \textit{black}.

The slicing of the first path prunes branches \textit{b_1}, \textit{b_4}, and \textit{b_5}, which means the paths along the pruned branches are redundant for verification. Branch \textit{b_1} can be pruned according to path slicing [27]. The reason is that there is no events transitiively data or control depend on \textit{n}, which means changing the value of \textit{n} cannot generate new event sequences. On the other hand, the reason for pruning \textit{b_4} and \textit{b_5} is the intersection of \textit{Preset} and \textit{Postset} is empty, which implies no counterexample paths along these branches exist. Both of \textit{b_2} and \textit{b_3} have the same result of intersecting \textit{Preset} and \textit{Postset}. In this situation, SRV will select the deeper branch, \textit{i.e}, \textit{b_3}, to explore. The path condition for generating the next input is \textit{m} ≤ 10 \land \textit{arr}[0] > 0 \land \textit{arr}[0] >= 100. Through solving the new path condition, we assume that the generated input is \langle \textit{arr} = [100, 2], \textit{m}=3 \rangle. The second iteration generates an accepted event sequence ⟨\textit{iterator}, \textit{update}, hasNext, next⟩. Thus, the path is a counterexample path.

Figure 4 shows the execution tree after the second iteration. For brevity, we omit the pruned candidate branches and states generated in the first iteration. Note that the second path terminates in the accepted state \textit{s_6}, because a runtime property violation happens. For branch \textit{b_2}, with the help of our property-oriented slicing method, we can infer that all possible event sequences along \textit{b_2} accepted by FSM_{\textit{arr}} are equivalent to the one explored in the second iteration, \textit{i.e}, \langle \textit{iterator}, \textit{update}, hasNext, next⟩. Hence, \textit{b_2} can be pruned.

In total, SRV needs two iterations to explore the full path space and finds the counterexample path in the second iteration regardless of \textit{arr}'s size. If we use depth-first search (DFS) or breadth-first search (BFS), the exploration will get stuck due to unfolding the two loops, failing to quickly find the counterexample path. If we use pure path slicing [27], only branch \textit{b_1} can be pruned, and the exploration will also get stuck due to the two loops. If we use pure regular property guiding [49], it will find the counterexample path during the second iteration, but no path pruning happens, hence it fails to complete the path exploration.
3 SRV: SYMBOLIC REGULAR VERIFICATION

This section presents the technical details of SRV. It first presents the overall synergic verification framework, then the two combined techniques, and finally discusses SRV.

3.1 Synergic Verification Framework

SRV’s key insight is to use slicing w.r.t. \( \varphi \) to prune redundant program paths, and the guiding method in [49] to find counterexamples earlier. More precisely, in addition to the synergy between slicing and guiding, (1) SRV’s property-oriented slicing method can prune additional paths through exploiting the guiding information, i.e., Preset and Postset, compared with path slicing [27]; and (2) SRV enhances the guiding method [49] with the support of multi-object regular properties. SRV aims for full verification, which means exploring the program’s whole path space to successfully verify the program or find all inequivalent violations of the property.

Algorithm 1: DSE-based Regular Property Verification

\[
\text{SRV}(P, M_{\varphi}, l_0) \\
\text{Data: program } P, \text{ FSM } M_{\varphi} \text{ and an initial input } l_0 \\
\begin{array}{l}
\text{worklist} \leftarrow \emptyset; \quad PC \leftarrow \text{false}; \quad I \leftarrow l_0; \\
\text{Postset} \leftarrow \text{ComputeFutureInfo}(P, M_{\varphi}); \\
\text{while true do} \\
\quad (PC, path_c, \text{Preset}) \leftarrow \text{runAndMonitor}(I, M_{\varphi}); \\
\quad \text{if accept}(M_{\varphi}, \text{Seq}(path_c)) \text{ then} \\
\quad \quad X \leftarrow X \cup \{\text{LSeq}(path_c)\}; \\
\quad \quad \text{Report a counterexample path;} \\
\quad R_s \leftarrow \text{Slice}(P, path_c, M_{\varphi}, \text{Preset}, \text{Postset}); \\
\quad \text{update(worklist, } R_s, \text{PC}); \\
\quad \text{if worklist } = 0 \lor \text{Timeout then} \\
\quad \quad \text{exit;} \\
\quad \text{PC} \leftarrow \text{Select(worklist, Preset, Postset);} \\
\quad I \leftarrow \text{Solve}(PC); \\
\end{array}
\]

Algorithm 1 shows the overall framework of SRV. The input to SRV consists of a program \( P \), an FSM \( M_{\varphi} \) for the negation of the regular property \( \varphi \) to be verified and an initial input \( l_0 \) to \( P \). The algorithm first computes the Postset information of \( P \) w.r.t. \( M_{\varphi} \) (Line 3, cf. Section 3.2) that will be used by slicing and guiding later. It uses a worklist to store the branches to be explored and \( X \) to store the accepted event sequences. During the accepted event sequences, the algorithm runs \( P \) and checks the property on the fly (Line 5, cf. Section 3.3). Besides the path condition \( PC \), the current path \( path_c \) is also collected along with DSE. At the same time, the Preset information is also calculated for each branch along \( path_c \) w.r.t. \( M_{\varphi} \) (cf. Section 3.3). If \( path_c \) is a counterexample path (Line 6), we add \( \text{LSeq}(path_c) \), i.e., the generated event sequence with program location [37] information, to \( X \) and report \( path_c \). Once a path is terminated, the property-oriented path slicing algorithm Slice (cf. Algorithm 2) is invoked to prune branches along the path (Line 9). Then, update is invoked to save new branches to worklist and prune the branches in worklist according to the slicing result. Based on the heuristic value of each branch (cf. Section 3.5), Select selects a branch to generate the path condition for the next iteration (Line 13). The inputs of the next iteration can be generated by invoking a backend SMT solver (Line 14). The algorithm repeats this process until the worklist becomes empty or timeout (Lines 11&12).

3.2 Statically Compute Future Information

For slicing and guiding, we calculate the Postset for each static program location. We improve the Postset calculation method in [49] in two dimensions: (1) extending the flow functions in IFDS to support multi-object regular properties; and (2) enhancing the data facts and flow functions in IFDS to record encountered event sequences for a program location. For each location \( l \), the Postset contains two types of information: (1) from which states the rest program after \( l \) can drive \( M_{\varphi} \) to an accepted state; and (2) the generated event sequences after \( l \) that can drive a state to an accepted state.

More precisely, we first construct the reversed FSM (denoted by \( \tilde{M}_{\varphi} \)) [22] of \( M_{\varphi} \), which accepts the reversed ones of \( M_{\varphi} \)’s accepted paths. For example, Figure 5 shows \( \tilde{M}_{\varphi} \) of the FSM in Figure 2, and \( M_{\varphi} \) accepts \( (\text{i.next}, \text{a.iterator}) \) that is the reverse of \( (\text{a.iterator}, \text{i.next}) \) accepted by the FSM in Figure 2. Observe that one state of \( \tilde{M}_{\varphi} \) may correspond to a set of states of \( M_{\varphi} \). For example, Figure 5’s FSM has a state \( \{q_1, q_4, q_4\} \), which there exists a transition from state \( q_4 \). The transition means there exists a transition from state \( q_1 \) to state \( q_4 \) in the FSM in Figure 2.

![Figure 5: The reversed FSM of iterator bug.](image)

To calculate the Postset, we update the data facts during exploring the program statements according to the transitions in \( \tilde{M}_{\varphi} \) and merge the data facts at merging points in the control flow graph.

To make the Postset analysis inter-procedural, we carry out a data flow analysis on the program’s inter-procedural control flow...
graph (ICFG) w.r.t. \( \mathcal{M}_{\varphi} \). The data flow analysis is implemented by employing the IFDS framework [40].

For a multi-object property \( \varphi \) involving \( k \) objects, a data flow fact in IFDS is an element \((T_a, q, b, s)\) in the domain \( \bigcup_{1 \leq n \leq k} O^n \times S \times B \times E \) (denoted by \( D \)), where \( O \) is the set of the identities of static objects, i.e., the static locations of object creations [37], \( S \) is the state set of the reversed FSM \( \mathcal{M}_{\varphi} \) of \( \neg \varphi \), \( B \) is the set of the basic blocks in the program, and \( E \) is the set of event sequences. For example, a data fact \(((o_1, o_2), (q_1 \sim q_4), b, s)\) of a program location \( l \) means that 1) from state \( q \) the program after \( l \) can drive \( \mathcal{M}_{\varphi} \) to an accepted state, 2) the event sequence \( s \) can be generated by \( o_1 \) and \( o_2 \) after \( l \), and 3) \( s \) can drive \( \mathcal{M}_{\varphi} \) to an accepted state from \( q \).

The relationship between an event and its corresponding object can be obtained through checking whether the class or interface of the event corresponds to the type of the object. For example, there exists a data fact \(((o_1, o_2), (q_1 \sim q_4), b, (update, hasNext, next))\) in the Postset of Line 10 in the example program in Figure 1, where \( o_1 \) and \( o_2 \) represent the identity of the ArrayList and Iterator objects, and \( b \) is the corresponding basic block of Line 10. Obviously, \((update, hasNext, next)\) can drive state \( q_1 \) to the accepted state of the FSM in Figure 2, and \( hasNext \) is related to the ArrayList object, while \( hasNext \) and \( next \) are related to the Iterator object.

Two different typed static objects \( o_1 \) and \( o_2 \) are related if their types are specified by \( \varphi \). Take the motivation program for example, an Iterator object is related with an ArrayList object according to the property specification in Figure 2. Without loss of generality, we assume \( \varphi \) specifies two objects for brevity. There are four kinds of flow functions in IFDS: call-to-start, exit-to-return, call-to-return, and normal functions. The normal and exit-to-return functions do not have any influence on calculating Postset, and both of them are identity functions. If a method invocation statement does not produce any event, its call-to-start function is the identity function; otherwise, it is a killall function [40] that kills all the data facts. The call-to-return function \( f_{cr} : D \rightarrow D \) is the main one that drives the calculation of Postset.

For a method invocation statement \( \text{obj}.\text{meth}(\ldots) \), if the statement does not produce an event, its \( f_{cr} \) is the identity function. Otherwise, suppose the identity set of \( \text{obj} \) is \( O_\text{a} \), the produced event is \( e_1 \) that can make the transition from \( q_1 \) to \( q_2 \) in \( \mathcal{M}_{\varphi} \), and the block of the statement is \( b_\epsilon \), then \( f_{cr} \) is the smallest function [29] satisfying the following conditions, where \( s_1 \circ s_2 \) represents the concatenation of sequences \( s_1 \) and \( s_2 \):

- \( f_{cr} \) is only parametric with objects, and the related objects of \( \varphi \) when running \( P \) do not depend on the inputs. Hence, we can obtain sound results of computing events, and thus Postset is sound.

### 3.3 Compute History Information

Different from Postset, Preset is calculated dynamically. The Preset of a location contains the states that are reached via the execution from the program entry to the location. Similar to the guiding method [49], we adopt runtime verification [31] to calculate the Preset information. Note that we enhance the calculation method to support multi-object properties.

A runtime object is a sensitive object if the corresponding class or interface is specified by the property \( \varphi \), e.g., the sensitive objects of the property given by Figure 2 include the ArrayList object and the Iterator object. We create a monitor to monitor the method invocations of every sensitive object, and record the current state of each monitored object. Note that for a multi-object property, the monitors of related objects will be merged according to the property specification. Preset is a set of monitors. Formally, we use \((I_s, q)\) to represent a monitor, where \( I_s \) is a set of object identities, and \( q \) is a state of the FSM \( \mathcal{M}_{\varphi} \). If any object’s method invocation results in an event of \( \mathcal{M}_{\varphi} \), the monitor performs a state transition w.r.t. \( \mathcal{M}_{\varphi} \) to compute Preset, which we formalize as

\[
(I_s, q) \xrightarrow{a_e} (I_s, q_2)
\]

where \( a \in I_s \), and state \( q_1 \in \mathcal{M}_{\varphi} \) is transitioned to state \( q_2 \) by event \( e \) generated by the method invocation on the object identified by \( a \).
For a multi-object property, a monitor’s sensitive objects are not created simultaneously. Suppose sensitive object \( o \) produces event \( e_1 \), if \( o \) is related to the objects in \( I_s \) w.r.t. the property \( \phi \) and \( o \not\in I_s \), following rule is used, where \( e_1 \) makes a transition from \( q_1 \) to \( q_2 \):

\[
(I_s, q_1) \xrightarrow{o, e_1} (I_s \cup \{o\}, q_2)
\]  

(2)

Take the second iteration of the motivation program (cf. Figure 4) for example, and suppose \( o_1 \) and \( o_2 \) represent the identities of the ArrayList and Iterator objects, respectively. Obviously, the encountered event sequence at Line 11 is \((o_1.\text{iterator}, o_1.\text{remove})\). As a result, according to the FSM in Figure 2, the Preset of location line 11 is \(((o_1, o_2), q_3)\).

For a given branch \( b \), the soundness of history information means that Preset contains all the reached states from the initial state via the path from the beginning to the program to branch \( b \).

**Theorem 3.2.** Given a program \( P \) and a regular property \( \phi \), if the sensitive objects of \( P \) are not data-dependent on the inputs, Preset is sound.

**Proof.** Recall that we compute the history information along with DSE, and Preset is calculated as the reached state set of the other branch of \( b \), denoted by \( \neg b \), executed in the current path. Suppose the corresponding event sequence to \( \neg b \) is \((a_0, a_1, \ldots, a_k, b_i)\), where \( i \geq 0 \). Because the sensitive objects do not depend on the inputs, the event sequence of \( b \) is the same as that of \( \neg b \). Hence, Preset of \( b \) contains the same reached states of \( \neg b \), which implies the soundness of Preset.

A static object is identified by its creation location. We relate a runtime object with a static object by their creation locations. Given the Preset and Postset of a branch \( b \), there intersection, denoted by \( \text{Preset}(b) \cap \text{Postset}(b) \), is defined as follows, where \( S(I_s) \) represents the set of the creation locations of the objects identified by \( I_s \), \( S(T_a) \) denotes the set of all elements in tuple \( T_a \), and \( M(X_1, X_2) \) denotes \( X_1 \subseteq X_2 \vee X_2 \subseteq X_1 \).

\[
\{q \mid (I_s, q) \in \text{Preset}, (T_a, q_r, b, s) \in \text{Postset} \land M(S(I_s), S(T_a)) \land q \in q_r\}
\]  

(3)

Take the candidate branch \( b_1 \) in the first iteration of the motivation program (cf. Figure 3) for example. There exists a data fact, i.e., \(((a_1, a_2), (q_1 \rightarrow q_2), b, \{U, H, N\})\), in the Postset below Line 10, where \( a_1 \) and \( a_2 \) correspond to the identities of the static ArrayList and Iterator objects, respectively. The computed Preset at Line 10 is \(((a_1, a_2, q_1), a_1), \) where \( a_1 \) and \( a_2 \) represent the ArrayList object and Iterator object, respectively. Clearly, the set of the creation locations of \( a_1 \) and \( a_2 \) is equal to \((a_1, a_2)\). Besides, since \( q_1 \in \{q_1 \sim q_4\} \), we have \( q_1 \) in the intersection of Preset and Postset.

### 3.4 Regular Property-Oriented Path Slicing

We now describe the algorithm for regular property-oriented path slicing, which is based on path slicing [27]. Specifically, our slicing algorithm enhances path slicing through exploiting the guiding information, i.e., Preset and Postset, to prune additional branches.

Before elaborating the slicing algorithm, we first give the definition of the equivalence relation of event sequences. An FSM \( M \) is a triple \((\Sigma, Q, q_0, \delta, F)\), where \( \Sigma \) is the event alphabet, \( Q \) is the state set, \( q_0 \) is the initial state, \( \delta : Q \times \Sigma \rightarrow Q \) is the transition function, and \( F \) is the set of accepted states. An event sequence \( s = (e_1, \ldots, e_n) \) \((n \geq 1)\) is accepted by \( M \) if for each \( e_i \), where \( 1 \leq i \leq n \), there exists \( q_i \in Q \) such that \((q_{i-1}, e_i, q_i) \in \delta \), and \( q_n \in F \). We use \( \mathcal{R}(s) \) to denote the event sequence after removing any event \( e_k \) in \( s \) that makes a self-circled transition, i.e., \((q_{k-1}, e_k, q_k) \in \delta \) and \( q_{k-1} \) is equal to \( q_k \).

**Definition 3.1.** Given an FSM \( M \) and two accepted event sequence \( s_1 \) and \( s_2 \) of \( M \), \( s_1 \) and \( s_2 \) are equivalent (denoted by \( s_1 \equiv_{M} s_2 \)) iff \( \mathcal{R}(s_1) = \mathcal{R}(s_2) \).

For example, the sequences \((\text{iterator}, \text{update}, \text{hasNext}, \text{next})\) and \((\text{iterator}, \text{update}, \text{hasNext}, \text{next}, \text{hasNext})\) are equivalent w.r.t. the FSM in Figure 2.

**Algorithm 2:** Regular Property-Oriented Path Slicing

\[
\begin{align*}
\text{Slice}(P, \text{path}_c, M_{\text{op}}, \text{Preset}, \text{Postset}) & \quad \text{Data: program } P, \text{ a path } \text{path}_c, \text{ and FSM } M_{\text{op}}. \\
\begin{alignat}{2}
1 & \begin{align*}
& \quad i \leftarrow \text{tail}(\mathcal{L}(\text{path}_c)); S \leftarrow \emptyset; \\
& \quad \text{while } i \neq \text{null do} \\
& \qquad \text{if } i \text{ is a branch instruction then} \\
& \qquad \quad \text{if } \text{Preset}(\neg i) \cap \text{Postset}(\neg i) \neq \emptyset \text{ then} \\
& \qquad \quad \quad T \leftarrow \text{Concatenate}(\neg i); \\
& \qquad \quad \quad \text{if } \exists (s_1) \in T, s_2 \in X \land (s_2 \equiv_{M_{\text{op}}} s_1) \text{ then} \\
& \qquad \quad \quad \quad \text{if } \exists e \in \text{Seq}(\text{path}_c) \text{ depends on } i \\
& \qquad \quad \quad \quad \quad \text{and } \neg i \text{ can reach any new event} \\
& \qquad \quad \quad \quad \quad \quad \text{then} \\
& \qquad \quad \quad \quad \quad \quad \quad S \leftarrow S \cup \{i\}; \\
& \quad \quad \text{else} \\
& \qquad \quad \quad \quad \text{if } \exists e \in \text{Seq}(\text{path}_c) \text{ depends on } i \\
& \qquad \quad \quad \quad \quad \quad \text{then} \\
& \qquad \quad \quad \quad \quad \quad \quad S \leftarrow S \cup \{i\}; \\
& \quad \quad \quad i \leftarrow \text{before}(i); \\
& \quad \quad \text{return } S; \\
\end{alignat}
\end{align*}
\]

Algorithm 2 gives our regular property-oriented path slicing. The input to the algorithm consists of the program \( P \) under verification, the current path \( \text{path}_c \), and the FSM \( M_{\text{op}} \) corresponding to the negation of the regular property to be verified. The algorithm processes the instructions in \( \text{path}_c \) in a backward manner, where \( \mathcal{L}(\text{path}_c) \) denotes the instruction list of \( \text{path}_c \). Finally, all the remaining instructions are stored in \( S \) and returned. The branches not in \( S \) are pruned.

For a branch instruction \( i \) in \( \mathcal{L}(\text{path}_c) \), we use \( \neg i \) to represent \( i \)’s branch not explored in \( \text{path}_c \). To decide whether \( i \) can be pruned, we exploit \( \text{Preset} \) and \( \text{Postset} \) in two ways. First, considering that both \( \text{Preset}(\neg i) \) and \( \text{Postset}(\neg i) \) are sound, the emptiness of their intersection implies that there exists no path along \( \neg i \) that can violate the property. Hence, we can slice branch \( i \) if \( \text{Preset}(\neg i) \cap \text{Postset}(\neg i) \) is empty (Lines 5). Second, we also prune branch \( i \) if all possible accepted event sequences of \( \neg i \) have an equivalent accepted event sequence explored before (Lines 6&7). The Concatenate operation concatenates the event sequence before \( \neg i \) (recorded during running) and the possible event sequences after \( \neg i \) (calculated in Postset), and produces an accepted event sequence set \( T \). If every sequence in \( T \) has an equivalent sequence in \( X \) (cf. Algorithm 1), which means that all the possible accepted event sequences along \( \neg i \) have been explored in an equivalent manner, \( i \) can be sliced. We also use the criteria in path slicing [27] to further slice the instructions.
that cannot alter the event sequence of the current path \(path_c\), i.e., a branch instruction \(i\) can be sliced if there is no event in \(Seq(path_c)\) transitively data- or control- depends on it and no new event can be reached along the direction of \(\neg i\) (Lines 8-10), similar rules also apply to the remaining types of instructions (Lines 12X13).

Path slicing [27] also slices a program execution path in a backward manner. More precisely, it keeps track of a set of variables (called live set) that determines the feasibility of the suffix of the path’s event sequence and the latest remained instruction (called step location). A branch instruction \(i\) will be remained if one of the following three conditions is satisfied. (1) \(\neg i\) can bypass the step location; and (2) there exists a path in the direction of \(\neg i\) that can modify the sensitive variables in live set; and (3) there exists a path in the direction of \(\neg i\) that can reach a new event. Actually, the first two conditions correspond to transitive data and control dependence, respectively. On the other hand, a normal instruction will be remained if it can modify the variables in live set.

Concatenation. The insight of concatenation is to infer the possible accepted event sequences of a branch \(br\) based on \(Preset(br)\) and \(Postset(br)\). For an element \((T_a, q_r, b, s)\) in \(Postset(br)\), we use \(Aes(br, q)\) to represent the set of statically calculated event sequences that can drive \(q\) to an accepted state, which can be derived from \(Postset\) as follows, where \(D_c\) is the set of calculated data facts during data flow analysis and \(D_c \subseteq D\).

\[
Aes(br, q) = \{s_1 \mid (T_a, q_r, b, s_1) \in D_c \land q \in q_r\}
\]

Then, we define \(\text{Concatenate}(br)\) as the following set

\[
\{s_1 \circ s_2 \mid \exists q \in \text{Preset}(br) \land \text{Postset}(br) \bullet s_2 \in Aes(br, q)\}
\]

where \(s_1\) is the event sequence before \(br\). A natural way to obtain the accepted event sequences along \(br\) is to concatenate the event sequence produced before \(br\) and the event sequences in \(Aes(br, q)\).

In principle, to ensure the soundness of slicing, both \(s_1\) and \(Aes(br, q)\) need to be context and flow sensitive [37]. In practice, \(Aes(br, q)\) is flow-sensitive, but not context-sensitive. We check the equivalence relation \(\text{wrt. a location sensitive variant of } M_{-\varphi}\), denoted by \(M_{\varphi}^{L}\). The intuition is that the reasons of the bugs caused by the same statement under different contexts tend to be the same. \(M_{\varphi}^{L}\) can be computed according to the program \(P\) in two steps. First, we collect all possible static locations for every event by an inter-procedural control flow analysis. Second, we replace every transition with the transitions of location sensitive events.

In the illustration example, after the second iteration (cf. Figure 4), the accepted sequence \((\text{iterators, update}_{11}, \text{hasNext}_{12}, \text{next}_{13})\) is added to \(X\). \(M_{\varphi}^{L}\) is the FSM after replace the event of each transition in Figure 2 by the event with location information. Then, according to the \(Preset\) and \(Postset\) of \(b_2\), \(Preset(b_2) \land Postset(b_2)\) only contains \(q_1\). Based on the example in Section 3.2, \(Aes(b_2, q_1)\) has four event sequences. Besides, the sequence before \(b_2\) is \((\text{iterators})\). Hence, \(\text{Concatenate}(b_2)\) contains four accepted event sequences, each of which is equivalent to \((\text{iterators, update}_{11}, \text{hasNext}_{12}, \text{next}_{13})\) \text{wrt. } M_{\varphi}^{L}\). Therefore, \(b_2\) is pruned.

3.5 Branch Selection

For a regular property \(\varphi\), only the relevant paths with specific event sequences can violate \(\varphi\). It is desirable to evaluate a branch’s probability of generating the accepted paths \text{w.r.t. } M_{-\varphi}. Then, after slicing, the branch with a higher probability will be selected first, in order to find counter-example paths earlier. Same as the regular property guided DSE [49], we use the size of \(\text{Postset} \cap \text{Preset}\) as the main heuristic value for evaluating a branch. When two branches have the same size of \(\text{Postset} \cap \text{Preset}\), the deeper one will be selected for efficient exploration.

3.6 Discussions

In principle, slicing and guiding are the orthogonal techniques that are synergistically combined in SRV. Slicing prunes irrelevant and equivalent relevant paths during DSE, while guiding boosts finding counterexample paths. Both are important for boosting verification. Since slicing is used when a path is completed, the effectiveness of slicing is related to how fast completed paths are generated. For example, if there exist very short paths in a program, BFS may be a good choice. On the other hand, guiding is insensitive to the search strategy. Without any knowledge of the shape of the path space, we integrate these two techniques with the DFS strategy.

In addition to their compatibility, slicing can boost the efficiency of property guiding. Finding accepted paths may be hindered by exploring relevant paths due to the imprecision of the guiding method. With the help of slicing, after one path is explored, the equivalent ones of the path can be pruned. Therefore, compared with pure guiding, SRV tends to find counterexamples faster.

Since slicing performs static analysis, its overhead may be high, e.g., when the path is long and the control flow graph is complex. To improve the performance, we perform slicing selectively based on the history results of slicing. The intuition is the locality of program paths, i.e., if a branch cannot be pruned, it tends not to be pruned either along the nearby paths. If the branch of any constraint in the current path is pruned at last time or first encountered, slicing would be carried out. With the help of such a lightweight dynamic prediction, we can reduce the effort of slicing, achieving a good balance between path pruning and slicing overhead.

Theorems 3.1&3.2 give sufficient conditions for the soundness of \(\text{Preset}\) and \(\text{Postset}\), respectively. Even though, there still exist a large number of programs and programs satisfying such conditions, e.g., the ones used in our experiment. However, considering our approach for computing the event sequences in \(\text{Postset}\) is not context sensitive, SRV is not sound, i.e., SRV may miss bugs resulting from different contexts but having same static location. We believe SRV is practical, because the root causes for the bugs of the same statement under different contexts tend to be the same.

4 IMPLEMENTATION AND EVALUATION

We have realized a prototype of SRV based on a regular property guided DSE tool [47], which is implemented on the DSE engine JPF-JDart [26] and WALA [24] static analysis platform. We have developed a property-oriented path slicer for Java bytecode based on Javaslicer [15], i.e., a dynamic slicing [45] tool.

We evaluate SRV along two dimensions:

- **Effectiveness and efficiency of SRV.** Can SRV effectively verify regular properties for real-world Java programs? How efficient is SRV compared with DFS, pure guiding and pure slicing?
- **Synergy between slicing and guiding.** Can slicing boost guiding in finding counterexample paths? How significant is the improvement?
4.1 Evaluation Setup

Table 1 lists the programs in our evaluation, which are all real-world open-source Java programs, totaling 259K lines of code (LOC). Rhino-a and soot-c come from the Ashes benchmark suite. JLex is a Java lexical analyzer. Bloat is from the DaCapo benchmark suite [6]. BMPDecoder is a decoder for BMP files. FTPClient is an FTP client. The six programs, pobs, jpat, jericho, nano-xml, htmlparser, and xml, are parser programs. The remaining, i.e., fastjason, jep, and udl, are library programs.

Table 1: Programs in the experiments

<table>
<thead>
<tr>
<th>Program</th>
<th>LOC</th>
<th>Brief Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>rhino-a</td>
<td>19799</td>
<td>Javascript interpreter</td>
</tr>
<tr>
<td>soot-c</td>
<td>32358</td>
<td>Static analysis editor</td>
</tr>
<tr>
<td>jlex</td>
<td>4400</td>
<td>Lexical analyzer</td>
</tr>
<tr>
<td>bloat</td>
<td>45357</td>
<td>Java bytecode optimization</td>
</tr>
<tr>
<td>bmpdecoder</td>
<td>531</td>
<td>BMP file decoder</td>
</tr>
<tr>
<td>ftpclient</td>
<td>2436</td>
<td>FTP client in Java</td>
</tr>
<tr>
<td>pobs</td>
<td>5488</td>
<td>Java parser objects</td>
</tr>
<tr>
<td>jpat</td>
<td>3254</td>
<td>Java string parser</td>
</tr>
<tr>
<td>jericho</td>
<td>25657</td>
<td>Jericho HTML Parser</td>
</tr>
<tr>
<td>nano-xml</td>
<td>3317</td>
<td>Non-Validating XML parser</td>
</tr>
<tr>
<td>htmlparser</td>
<td>21830</td>
<td>HTML parser in Java</td>
</tr>
<tr>
<td>xml</td>
<td>5138</td>
<td>XML parser in Java</td>
</tr>
<tr>
<td>fastjason</td>
<td>20223</td>
<td>JSON library from alibaba</td>
</tr>
<tr>
<td>jep</td>
<td>42868</td>
<td>Mathematics library</td>
</tr>
<tr>
<td>udl</td>
<td>26896</td>
<td>UDL language library</td>
</tr>
<tr>
<td>Total</td>
<td>259642</td>
<td>15 open source programs</td>
</tr>
</tbody>
</table>

As Table 2 shows, we applied SRV to verify widely-used regular properties, including both single- and multi-object ones. Properties with superscript * are multi-object ones; the remaining are single object properties. In addition, we also verify some user-defined properties. For example, the property we defined for htmlparser requires that the input string is in the JSP format, i.e., "< % . . . > ".

Table 2: Regular properties in the experiments

<table>
<thead>
<tr>
<th>Property</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>Enumeration</td>
<td>Call hasMoreElements before nextElement</td>
</tr>
<tr>
<td>Iterator</td>
<td>Call hasNext before next</td>
</tr>
<tr>
<td>Reader</td>
<td>Do not update the collection while iterating</td>
</tr>
<tr>
<td>Writer</td>
<td>Do not write a closed stream</td>
</tr>
<tr>
<td>Socket</td>
<td>Do not use a closed socket</td>
</tr>
</tbody>
</table>

Since most of the programs are violation free, to further evaluate our method, we mutate [28] the programs. First, we collect all the branch statements along DSE, then we randomly select a branch to automatically inject an event, e.g., a close operation for the Reader property. We generate three mutants for each program, except for those with user-defined properties. Note that such injections may not necessarily lead to real violations.

An evaluation task comprises a program and a property. A task was run in four modes: DFS (D), pure guiding (G), pure path slicing (S) and SRV (S'). Under each mode, the time limit is 1 hour. All the experiments are carried out on the identical servers, each of which has 256GB RAM and four 2.13GHz XEON CPUs with 32 cores.

4.2 Evaluation Results

Table 3 lists evaluation results. The first column gives the verification tasks, including the names of the programs and the verified properties, where a multi-object property has a superscript *. The second column Type indicates whether an analyzed program has been mutated or not, with O represents the original program, and bug, the i-th mutant. The column Total Time(s) lists time consumed for each verification task in four modes, where T0 represents time-out. In our evaluation, completing a verification means having explored all the path space. The time for finding the first counterexample is shown in the column First Violation Time(s), where NO means no counterexample path and NA represents unknown due to timeout.

Table 3 shows that SRV completes 30 tasks in 39, while DFS (D), pure guiding (G) and pure slicing (S) complete 22, 22 and 23 tasks, respectively. Compared with these alternatives, SRV achieves 36%, 36% and 30% improvement, respectively. For the successfully verified 30 tasks, SRV at least has an average 8.4X, 8.6X, and 7X speedups over DFS, pure guiding and pure slicing, respectively. We inspected the programs that SRV fails to verify, i.e., jLex, rhino-a, htmlparser, and xml, and found that those programs have complex and sensitive control flow. Most paths of those programs are relevant, and only a few paths are counterexample paths. As a result, the overhead of static analysis used in slicing and guiding becomes very high, and only a small part of path space can be pruned.

Figure 6 shows the relationship between the number of completed verification tasks and the time threshold. The X-axis varies the time threshold from five minutes to one hour, while the Y-axis is the number of completed verification tasks. SRV can complete the most tasks under a given time threshold. In addition, all the completed 30 tasks by SRV are completed within 5 minutes, demonstrating SRV’s efficiency.

To show the effectiveness of property guiding, we also collect the time for finding the first counterexample path. For the tasks in which violations exist, pure guiding is the most efficient to find the first violation. Due to the overhead of slicing, SRV is slower than pure guiding in most tasks, but has the same order of magnitude in time. Both SRV and pure guiding achieve orders of magnitude
speedups over DFS and pure path slicing in finding the first counterexamples. When a violation is very deep and there possibly exist a large number of relevant paths, it cannot be detected without slicing. For example, for fastjason, pure guiding fails to detect a violation within one hour, while SRV needs only 102.6 seconds. Within one hour, guiding and SRV can find a counterexample for 23 and 22 programs respectively, while DFS and pure path slicing can only find 15 and 13, indicating the effectiveness and efficiency of guiding.

Pruning branches with positive heuristic values can boost finding counterexamples. For the 24 tasks with counterexamples found, slicing can boost guiding by reducing the number of iterations for finding the first counterexample in 7 (29%) tasks. Notably, for fastjason, SRV needs only 5 iterations, but all the other modes fail to detect a violation after thousands of iterations. To inspect the boosting of slicing to guiding further, we collect the information of the pruned branches with positive heuristic values.

Figure 7 shows the improvement by synthesizing the results of all the tasks, where the X-axis is the path order for the first 2000 paths, and the Y-axis is the number of the pruned branches with a positive heuristic value for guiding. As shown in the figure, much of the boosting happens during the early stage, i.e., in the first 1500 paths, which indicates the necessity of selective slicing.

In addition, we collect the information about iterations, and the results show that SRV uses the fewest iterations to complete path exploration. Specifically, the iterations using our slicing algorithm is two orders of magnitude less than that using path slicing [27]. Furthermore, we adjust the time threshold to 24 hours for the failed tasks, and found that all the tasks were still failed to be verified, except that program jep can be verified in pure slicing mode.
5 RELATED WORK

The closest related work to SRV is regular property guided DSE [49] and Woodpecker [16]. Different from the objective of [49], i.e., finding an accepted path as soon as possible, SRV aims to quickly complete the path exploration of the program by employing slicing to prune redundant paths, and the slicing can also reduce the iterations for finding counterexample paths. Compared with Woodpecker [16], which uses path slicing [27] to prune redundant paths for verifying system rules via symbolic execution, as demonstrated by the evaluation results (cf. Section 4.2), SRV is more scalable because it can prune more paths and find violations faster. Meta Compilation (MC) [19, 20] is a scalable static approach to detecting violations of properties specified by a state machine language. MC is neither sound nor complete. ESP [17] is a path-sensitive static verifier for regular properties. ESP achieves strong scalability by merging symbolic states. However, ESP may produce false alarms due to imprecise modeling of program statements. In [21], a staged static ty pestate property [43] verification framework is proposed based on a parametric abstract domain. The false alarms can be eliminated gradually by the staged analysis. Clara [7] employs forward and backward data flow analysis to remove instrumentations for runtime monitoring of typestate properties. Our guiding method makes the backward analysis of Clara to be interprocedural for calculating Postset. Compared with static approaches, SRV enjoys completeness by trading scalability because it executes the program under verification.

Dynamic methods are mainly from runtime verification [31]. The basic procedure is to generate a monitor for verification from a property, and the monitor is usually implemented via instrumentations to the program. The verification takes place at runtime based on the information collected by instrumentations. Hence, dynamic approaches verify a single program path. JavaMOP [12] and Trace-matches [2] are representative tools for runtime verification of Java programs. The calculation of Preset uses the idea of monitoring in runtime verification, and the monitoring is implemented at the virtual machine level. Compared with dynamic approaches, SRV employs DSE to explore the path space of the program systematically, which improves code coverage and finds more bugs.

Software model checking has also been used for regular property verification. SLAM [4] uses predicate abstraction [5] to obtain an abstract model of a program. Then, at the model level, SLAM uses model checking to verify regular properties. When a counterexample is found by model checking, it is reported when it is a real violation; otherwise, the counterexample is used to refine the abstract model. YOGI [38] improves SLAM by integrating DSE to speed up model refinement and finding real counterexamples. Compared with these approaches, SRV is lightweight and scalable because it adopts efficient static analysis to boost verification. Furthermore, guiding and pruning are commonly investigated for improving the scalability of symbolic execution. For guiding symbolic execution, different methods are proposed w.r.t. different goals, including improving code coverage [9, 10, 32, 42, 44, 46], reaching a program location [3, 11, 34, 48], targeting the differences between two program versions [35, 39], aiming at the unverified path space [13], and generating a path satisfying a regular property [49]. On the other hand, pruning path space is also an effective method to mitigate path explosion. Same as guiding, the existing work on pruning also differs in their perspectives to decide redundancy, such as read-write information [8], assertion violation [25], and rule violation [16]. SRV extends the existing work by the synergy of guiding and pruning for verifying regular properties.

6 CONCLUSION

This paper presents symbolic regular verification, a practical DSE-based technique for verifying regular properties. To improve scalability, we introduce a synergistic combination of property-oriented path slicing and guiding. SRV’s property-oriented path slicing prunes redundant paths, while guiding helps finding counterexamples quickly. The two combined techniques not only complement, but also strengthen each other. We have developed a prototype of SRV for Java and evaluated it on real-world programs w.r.t. widely-used regular properties. Our extensive evaluation demonstrates that SRV is effective and efficient, and outperforms the state-of-the-art significantly for regular property verification. Interesting future work includes (1) techniques to further reduce slicing overhead and (2) further improvements to our tool’s usability and feasibility for releasing to and benefiting the community.

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REFERENCES


