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# Symbolic Verification of Message Passing Interface Programs

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**ETH** zürich



# High Performance Computing



# MPI Paradigm

- Key features of MPI Applications
  - Non-deterministic, e.g. wildcard receive
  - **Blocking** and **non-blocking** communications
  - Data and control intensive
- MPI programs are hard to develop and maintain

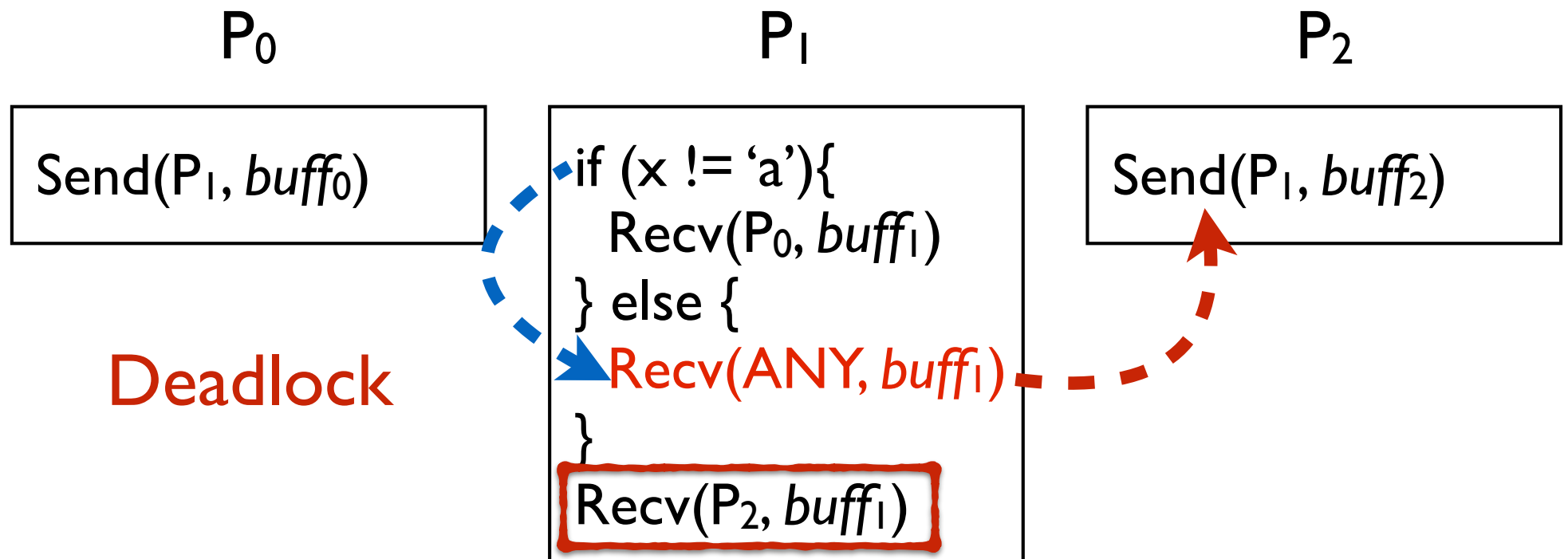
*Verifying MPI programs is challenging*

# Challenges

- Non-determinism (Soundness)
- Input && Schedule coverage

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- Non-determinism (Soundness)
- Input & Schedule coverage



# Existing Work of MPI Verification

|            | Automation | Input Coverage | Non-Blocking |
|------------|------------|----------------|--------------|
| CIVL(TASS) | Yes        | Yes            | No           |
| MOPPER     | Yes        | No             | Yes          |
| MPI-SPIN   | No         | Yes            | Yes          |

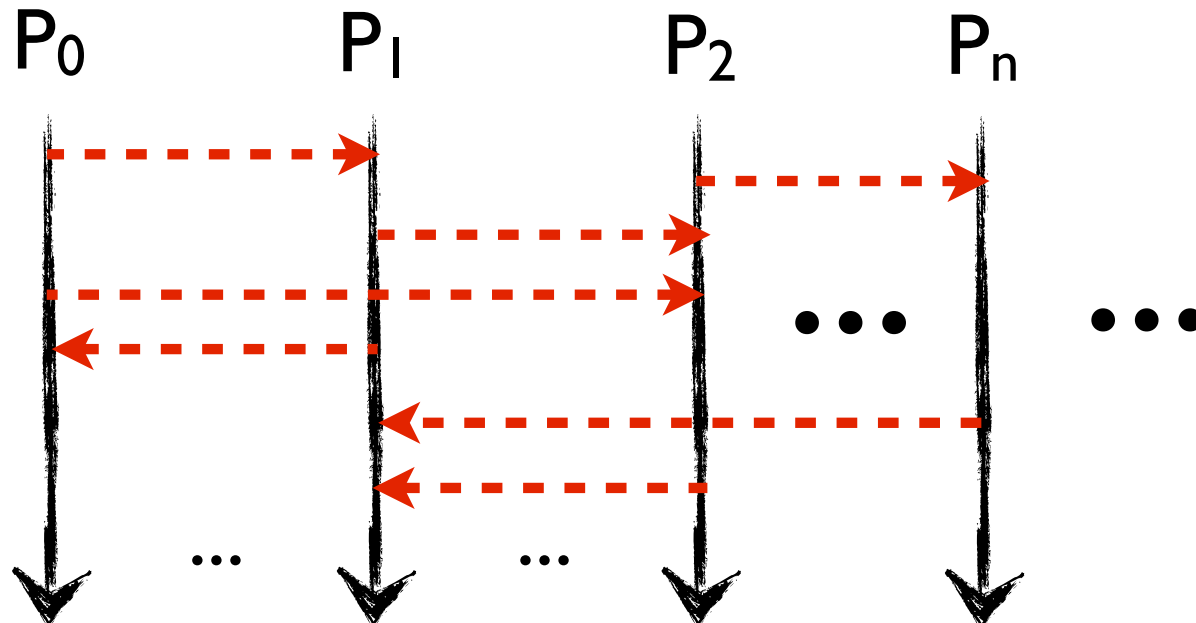
Either do not support **input-related verification** or fail to support the verification of **non-blocking** MPI programs

# Existing Work of MPI Verification

|                   | Automation | Input Coverage | Non-Blocking |
|-------------------|------------|----------------|--------------|
| <b>CIVL(TASS)</b> | Yes        | Yes            | No           |
| <b>MOPPER</b>     | Yes        | No             | Yes          |
| <b>MPI-SPIN</b>   | No         | Yes            | Yes          |
| <b>MPI-SV</b>     | Yes        | Yes            | Yes          |

# Challenges

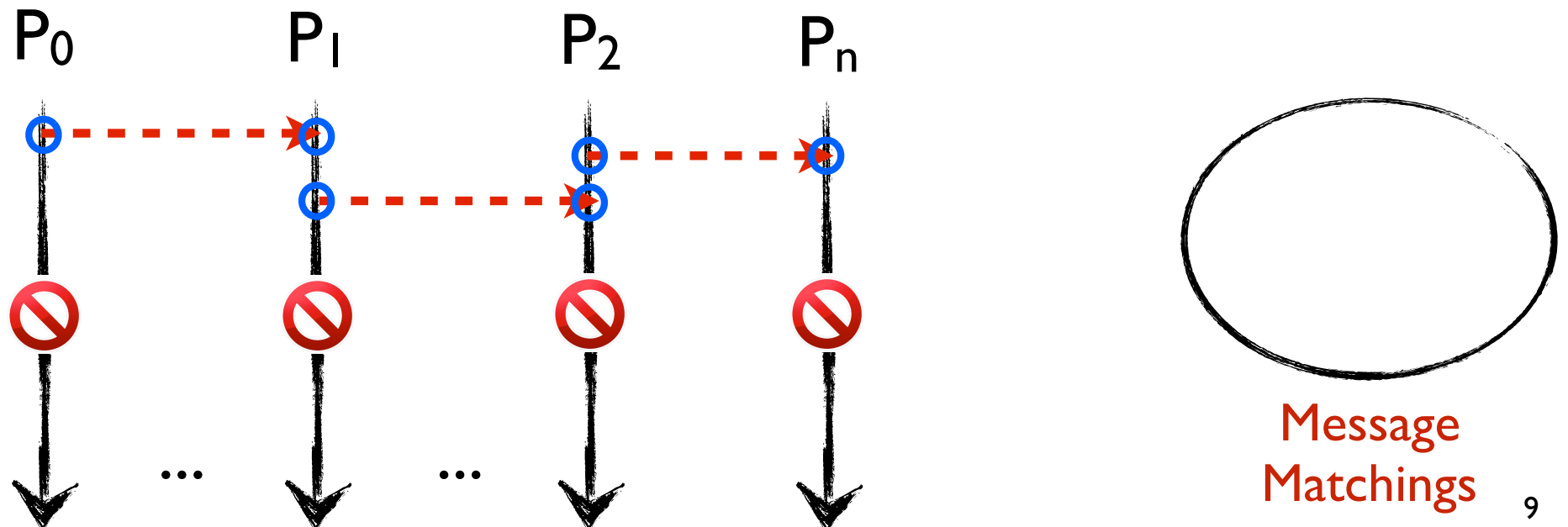
- The explosion of state space
  - Parallel execution, wildcard receive, branches
  - Exponential increasing





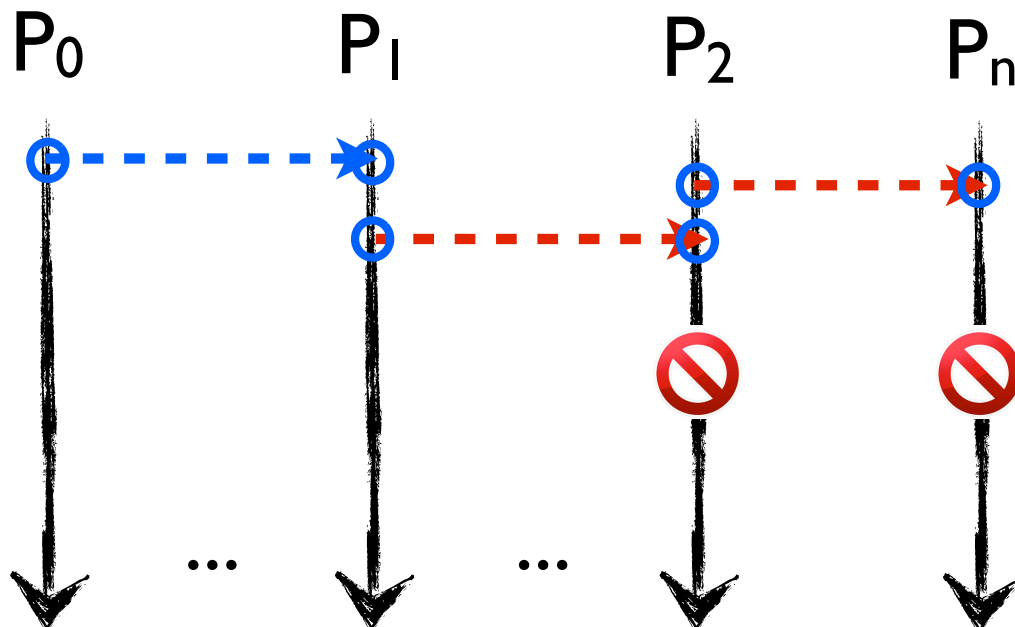
# Key Ideas (1/2)

- Challenge 1: non-determinism
  - Symbolic execution for input coverage
  - Blocking-driven matching of wildcard receives



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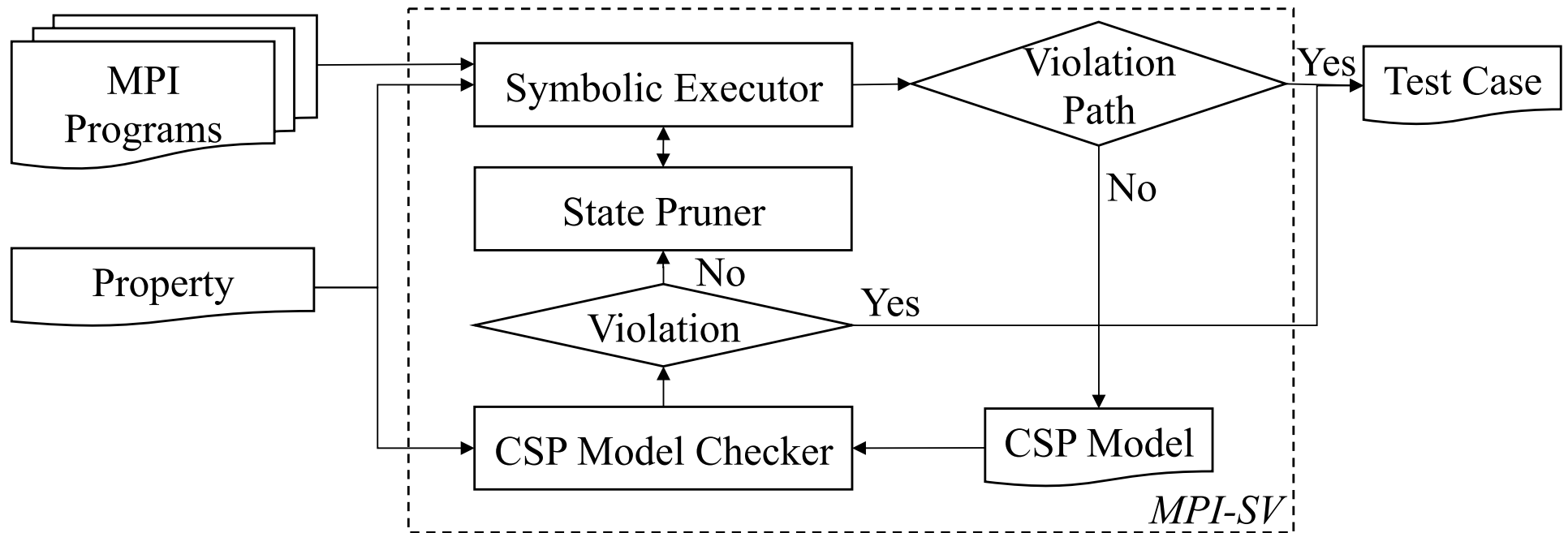
*The happens-before  
requirements in MPI  
standard are  
preserved*

# Key Ideas (2/2)

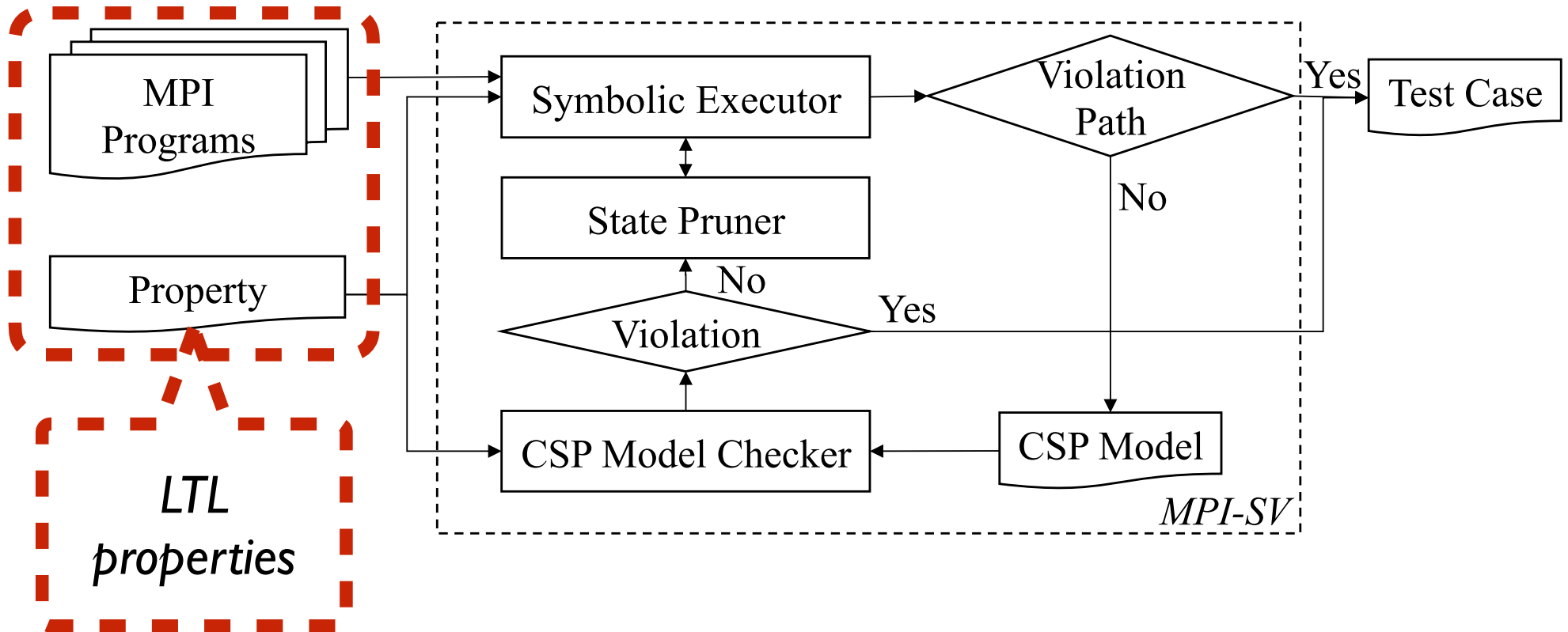
- Challenge 2: the explosion of state space
  - Partial order reduction
  - Model checking-based boosting



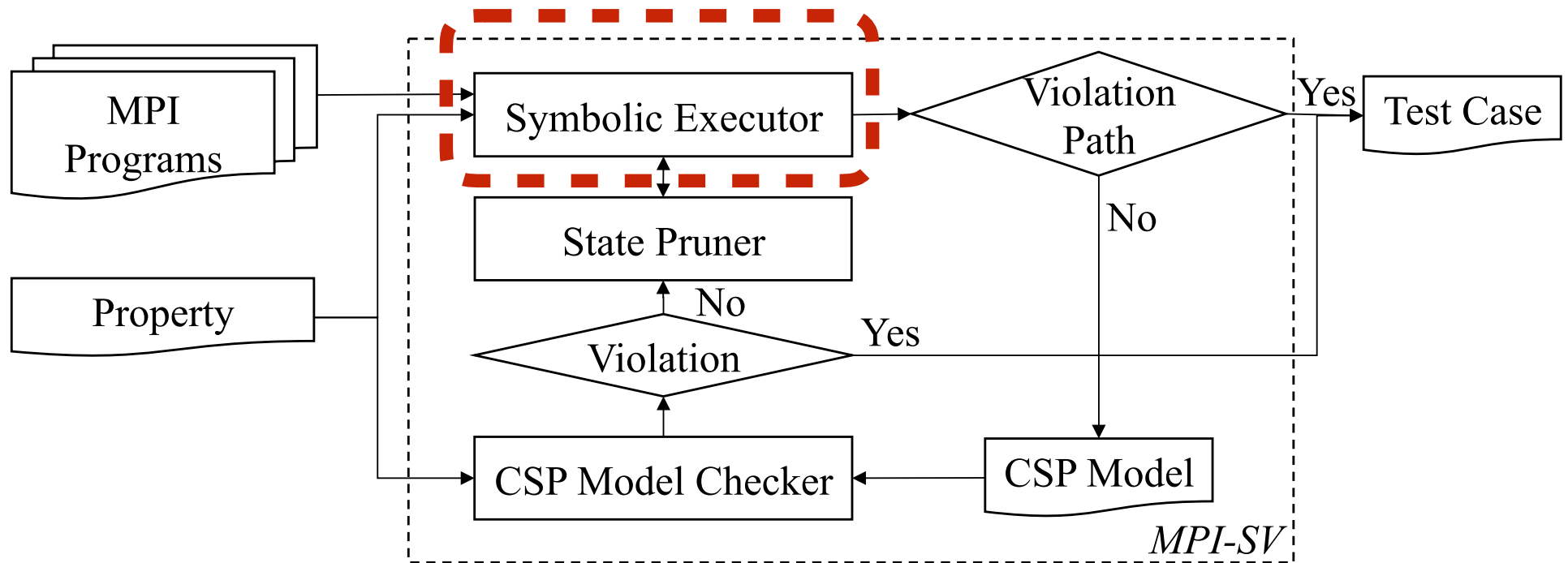
# Basic Framework



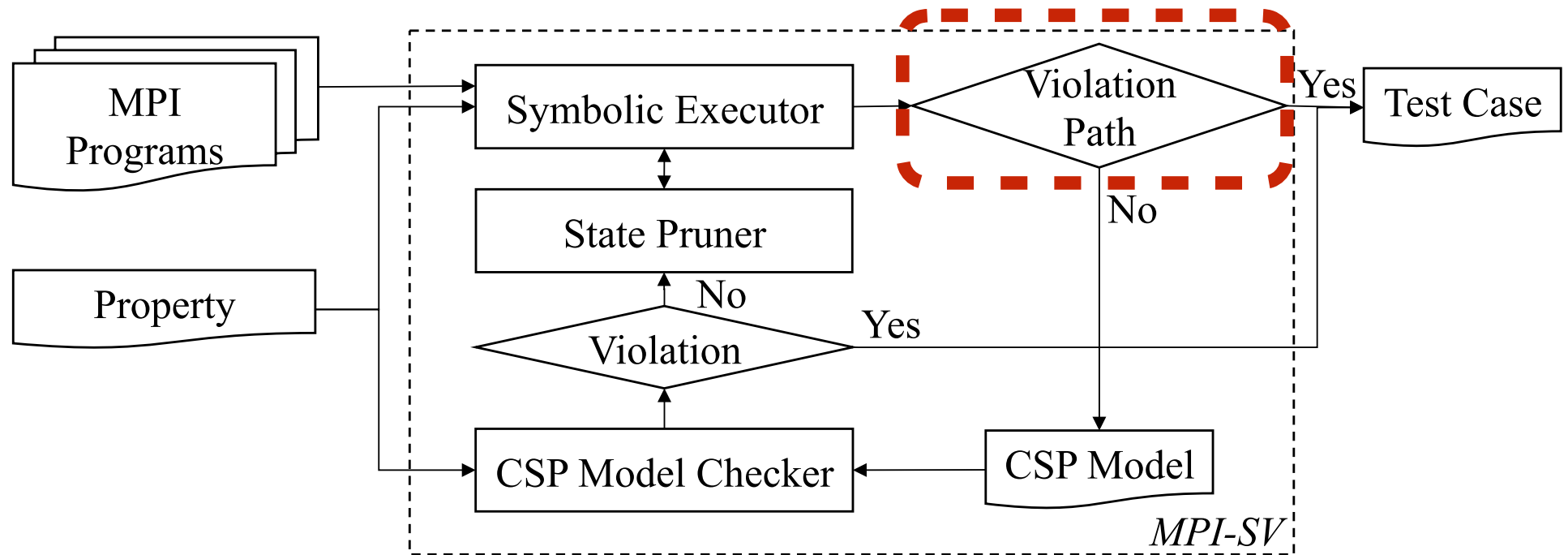
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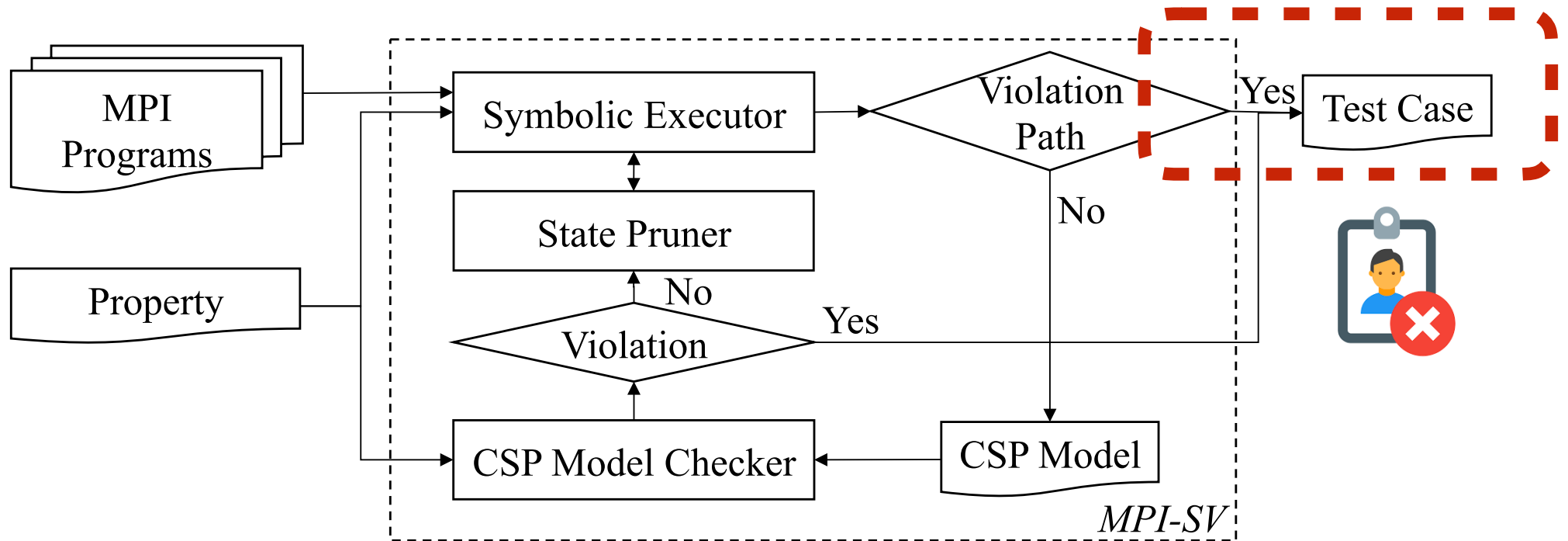
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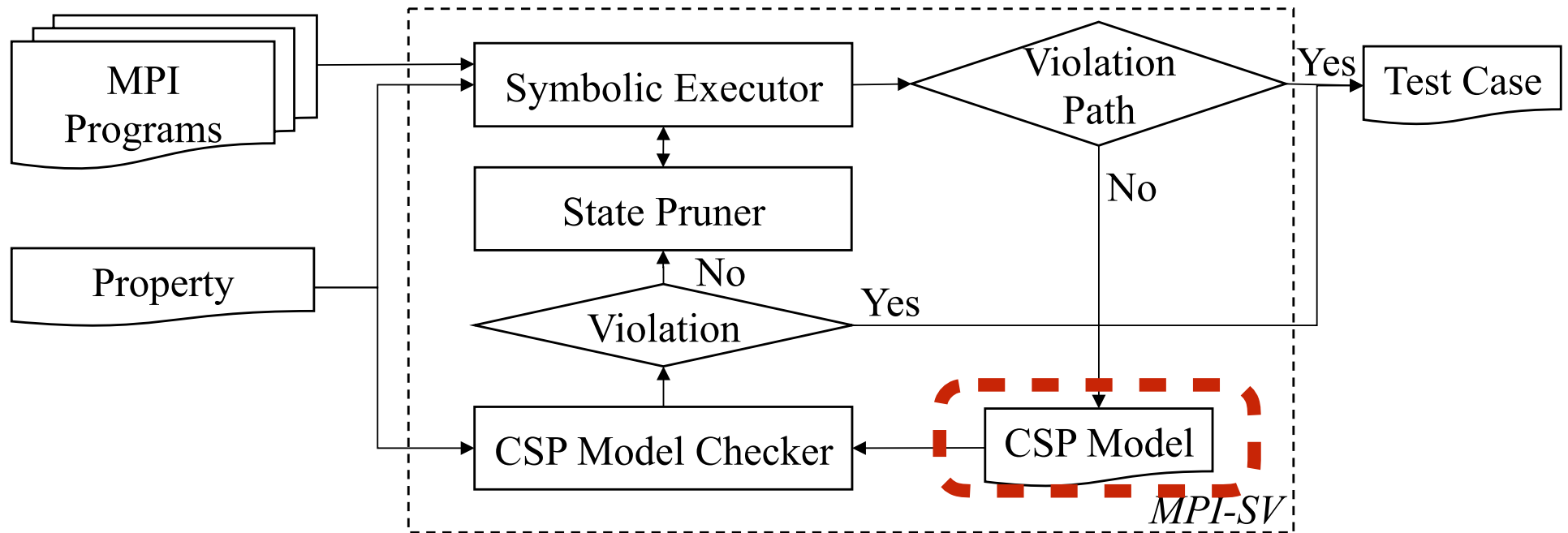


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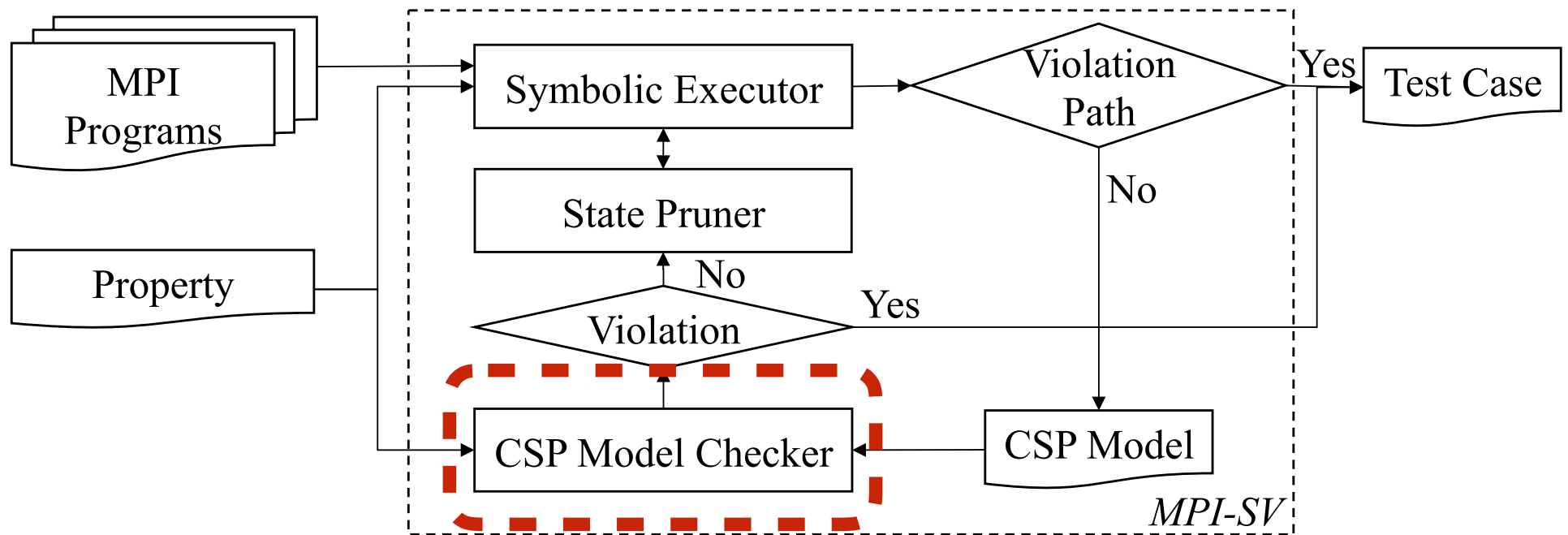




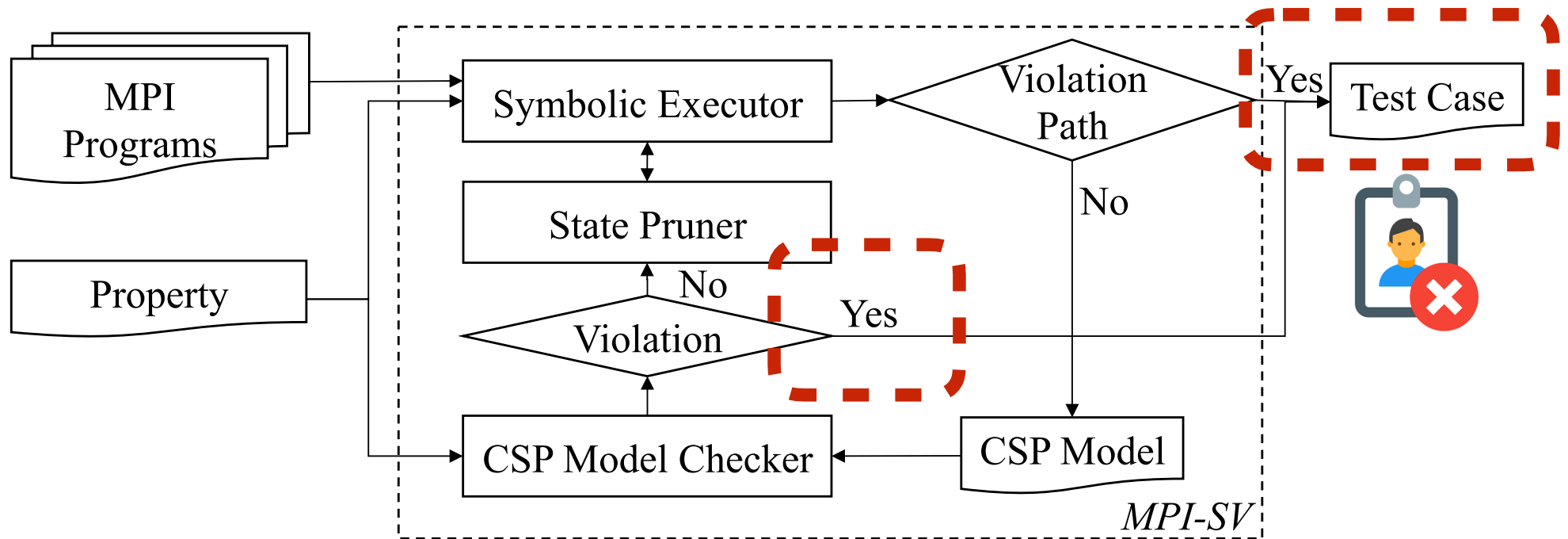
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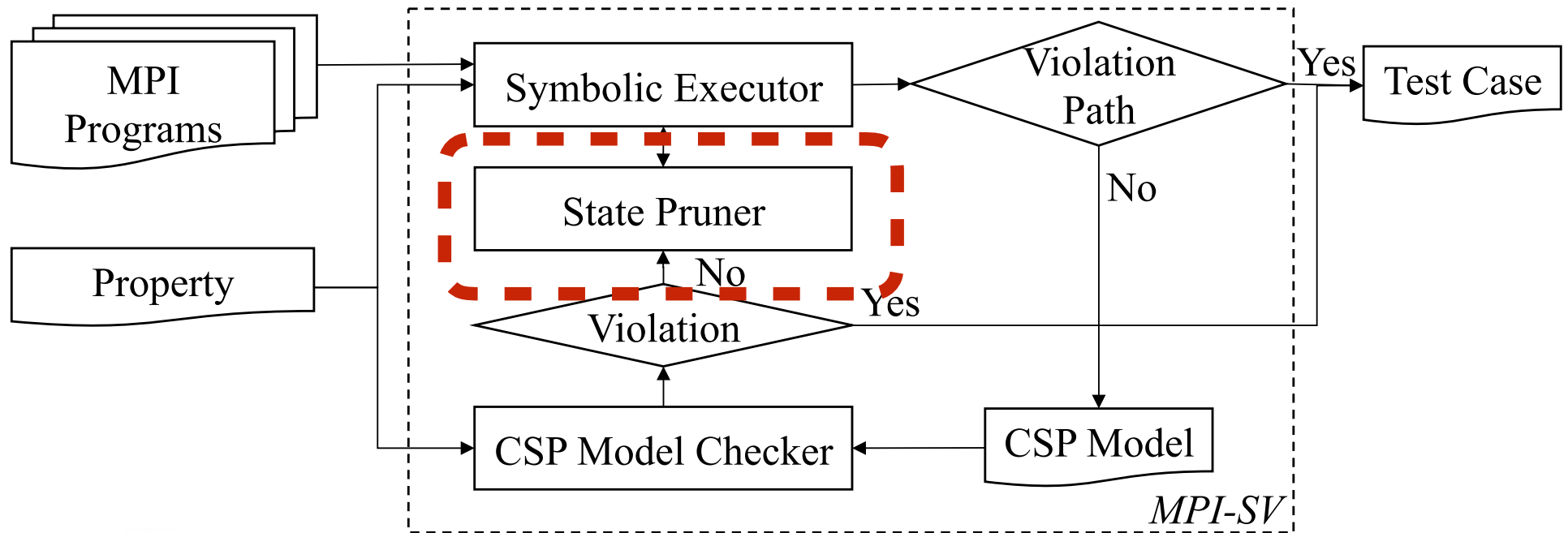


# Basic Framework



*CSP modeling is sound and complete*

# Basic Framework



*CSP modeling is sound and complete*

# High-Level View

*Automatic Model Extraction*



*Boosting*

*Enlarge the scope of verifiable properties*

# Experiments

- Property
  - *Deadlock freedom*
  - *Non-reachability properties*
- Analyze each task (program/property) in **one hour**

| Program      | LOC          | Description                        |
|--------------|--------------|------------------------------------|
| DTG          | 90           | Dependence transition group        |
| Matmat       | 105          | Matrix multiplication              |
| Integrate    | 181          | Integral computing                 |
| Diffusion2d  | 197          | Simulation of diffusion equation   |
| Gauss_elim   | 341          | Gaussian elimination               |
| Heat         | 613          | Heat equation solver               |
| Mandelbrot   | 268          | Mandelbrot set drawing             |
| Sorting      | 218          | Array sorting                      |
| Image_manip  | 360          | Image manipulation                 |
| DepSolver    | 8988         | Multimaterial electrostatic solver |
| Kfray        | 12728        | KF-Ray parallel raytracer          |
| ClusterW     | 23265        | Multiple sequence alignment        |
| <b>Total</b> | <b>47354</b> | <b>12 open source MPI programs</b> |

# Main Results

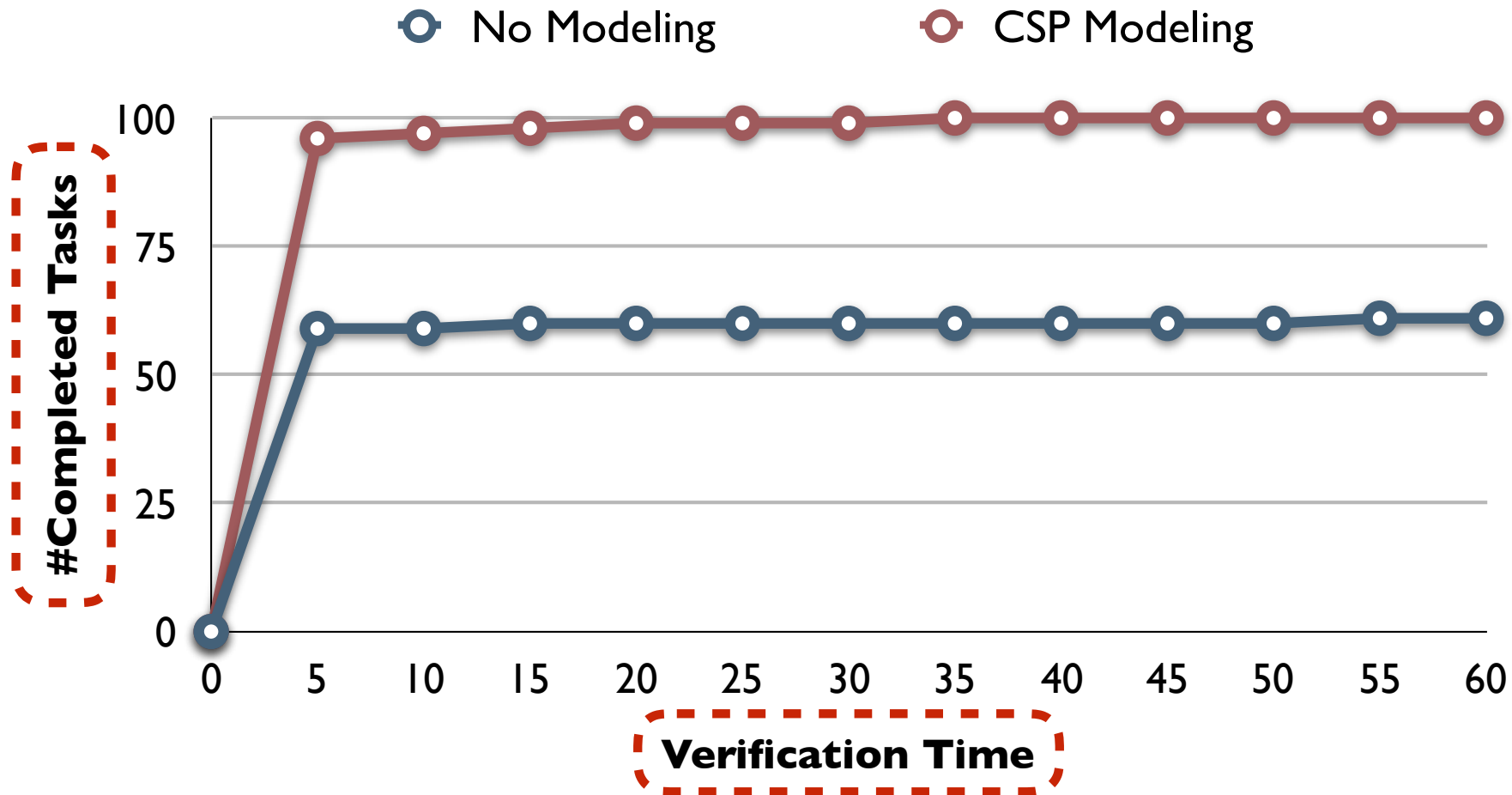
| Program (#Procs)    | T                     | Deadlock | Time(s)             |                     | #Iterations        |              |
|---------------------|-----------------------|----------|---------------------|---------------------|--------------------|--------------|
|                     |                       |          | Symbolic execution  | Our approach        | Symbolic execution | Our approach |
| DTG(5)              | <i>o</i>              | 0        | 10.12               | 9.02                | 3                  | 1            |
|                     | <i>m</i> <sub>1</sub> | 0        | 13.69               | 9.50                | 10                 | 2            |
|                     | <i>m</i> <sub>2</sub> | 1        | 10.02               | 8.93                | 4                  | 2            |
|                     | <i>m</i> <sub>3</sub> | 1        | 10.21               | 9.49                | 4                  | 2            |
|                     | <i>m</i> <sub>4</sub> | 1        | 10.08               | 9.19                | 4                  | 2            |
| Matmat*(4)          | <i>o</i>              | 0        | 9.04                | 9.29                | 2                  | 2            |
|                     | <i>o</i>              | 0        | 36.94               | 10.43               | 54                 | 1            |
| Integrate(6/8/10)   | <i>o</i>              | 0/0/0    | 78.17/to/to         | 8.87/10.45/44.00    | 120/1912/3162      | 1/1/1        |
|                     | <i>m</i> <sub>1</sub> | 0/0/-1   | to/to/to            | 49.94/to/to         | 4773/3712/5206     | 32/128/79    |
| Integrate*(4/6)     | <i>o</i>              | 1/1/1    | 9.35/9.83/9.94      | 9.39/10.76/44.09    | 2/2/2              | 2/2/2        |
|                     | <i>o</i>              | 0/0      | 24.18/123.55        | 9.39/32.03          | 27/125             | 1/1          |
| Diffusion2d(4/6)    | <i>o</i>              | 0/0      | 106.86/to           | 9.84/13.19          | 90/2041            | 1/1          |
|                     | <i>m</i> <sub>1</sub> | 0/1      | 110.25/11.95        | 10.18/13.81         | 90/2               | 1/2          |
|                     | <i>m</i> <sub>2</sub> | 0/1      | 3236.02/12.66       | 17.05/14.38         | 5850/3             | 16/2         |
|                     | <i>m</i> <sub>3</sub> | 0/0      | to/to               | 19.26/199.95        | 5590/4923          | 16/64        |
|                     | <i>m</i> <sub>4</sub> | 1/1      | 11.35/11.52         | 11.14/14.22         | 3/2                | 2/2          |
| Gauss_elim(6/8/10)  | <i>o</i>              | 1/0      | 10.98/to            | 10.85/13.44         | 2/1991             | 2/1          |
|                     | <i>o</i>              | 0/0/0    | to/to/to            | 13.47/15.12/87.45   | 2756/2055/1662     | 1/1/1        |
| Heat(6/8/10)        | <i>m</i> <sub>1</sub> | 1/1/1    | 155.40/to/to        | 14.31/16.99/88.79   | 121/2131/559       | 2/2/2        |
|                     | <i>o</i>              | 1/1/1    | 17.31/17.99/20.51   | 16.75/19.27/22.75   | 2/2/2              | 1/1/1        |
|                     | <i>m</i> <sub>1</sub> | 1/1/1    | 17.33/18.21/20.78   | 17.03/19.75/23.16   | 2/2/2              | 1/1/1        |
|                     | <i>m</i> <sub>2</sub> | 1/1/1    | 18.35/18.19/20.74   | 16.36/19.53/23.07   | 2/2/2              | 1/1/1        |
|                     | <i>m</i> <sub>3</sub> | 1/1/1    | 19.64/20.21/23.08   | 16.36/19.72/22.95   | 3/3/3              | 1/1/1        |
| Mandelbrot(6/8/10)  | <i>o</i>              | 0/0/0    | 97.69/118.72/141.87 | 18.68/23.84/27.89   | 96/96/96           | 4/4/4        |
|                     | <i>m</i> <sub>1</sub> | 1/1/1    | 12.92/15.80/15.59   | 14.15/14.53/16.86   | 2/2/2              | 2/2/2        |
| Mandelbrot*(4/6)    | <i>o</i>              | 0/0      | 94.17/116.5/148.38  | 97.19/123.36/151.83 | 4/4/4              | 4/4/4        |
|                     | <i>o</i>              | 0/0      | to/to/to            | 51.59/68.25/226.96  | 1054/981/1146      | 1/1/1        |
| Sorting*(4/6)       | <i>o</i>              | 0/0/0    | to/to/to            | 53.44/282.46        | 1301/1575          | 1/1          |
|                     | <i>o</i>              | 0/0/0    | to/to/to            | 47.28/79.38/238.37  | 1234/1105/1162     | 1/1/1        |
| Image_manip(6/8/10) | <i>o</i>              | 0/0/0    | to/to/to            | 47.94/80.10/266.16  | 1365/1127/982      | 1/1/1        |
|                     | <i>o</i>              | 0/0/0    | to/to/to            | 47.71/90.32/266.08  | 1241/1223/915      | 1/1/1        |
| DepSolver(6/8/10)   | <i>o</i>              | 0/0/0    | to/to/to            | 895.63/to/to        | 175/1342/866       | 5/17/2       |
|                     | <i>o</i>              | 0/0/0    | to/to/to            | 47.49/79.94/234.99  | 1347/1452/993      | 1/1/1        |
| Kfray(6/8/10)       | <i>o</i>              | 0/0/0    | to/to/to            | 47.75/80.33/223.77  | 1353/1289/1153     | 1/1/1        |
|                     | <i>o</i>              | 0/0      | to/to               | 53.44/282.46        | 1301/1575          | 1/1          |
| Kfray*(4/6)         | <i>o</i>              | 0/0      | to/to               | 47.28/79.38/238.37  | 1234/1105/1162     | 1/1/1        |
|                     | <i>o</i>              | 0/0      | to/to               | 47.94/80.10/266.16  | 1365/1127/982      | 1/1/1        |
| Clustalw(6/8/10)    | <i>o</i>              | 0/0      | to/to               | 47.71/90.32/266.08  | 1241/1223/915      | 1/1/1        |
|                     | <i>o</i>              | 0/0      | to/to               | 895.63/to/to        | 175/1342/866       | 5/17/2       |
| Clustalw*(4/6)      | <i>o</i>              | 0/0      | to/to               | 47.49/79.94/234.99  | 1347/1452/993      | 1/1/1        |
|                     | <i>o</i>              | 0/0      | to/to               | 47.75/80.33/223.77  | 1353/1289/1153     | 1/1/1        |

||| verification tasks

|             | No Modeling | CSP Modeling | Speedup |
|-------------|-------------|--------------|---------|
| Finished    | 61 (55%)    | 100 (90%)    |         |
| Deadlock    | 44          | 48           | >5X     |
| No Deadlock | 17          | 52           | >19X    |

MPI-SV is more effective and efficient than pure symbolic execution

# The Progress Distribution



MPI-SV can complete more tasks under the same time threshold



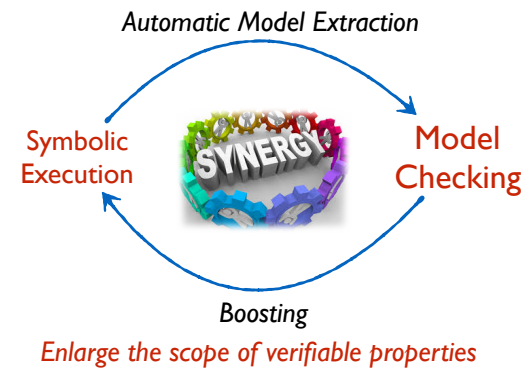
# Conclusion

## High Performance Computing



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## High-Level View



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## Existing Work of MPI Verification

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## Main Results

### III verification tasks

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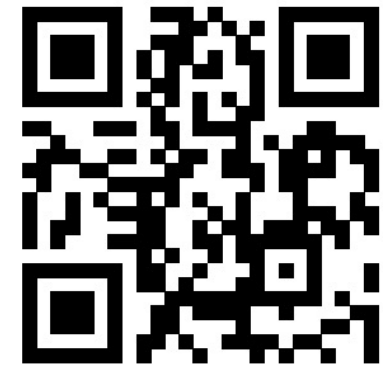


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Thank you!  
Q&A



<https://mpi-sv.github.io>

